

$$\mathbf{u}(t) = \begin{cases} 1 & , \ t > 0 \\ 1/2 & , \ t = 0 \\ 0 & , \ t < 0 \end{cases}$$

$$sgn(t) = \begin{cases} 1 & , t > 0 \\ 0 & , t = 0 \\ -1 & , t < 0 \end{cases}$$

$$ramp(t) = \begin{cases} t & , t \ge 0 \\ 0 & , t < 0 \end{cases}$$

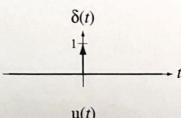
$$\delta_T(t) = \sum_{n = -\infty}^{\infty} \delta(t - nT)$$

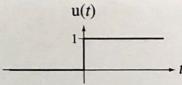
$$rect(t) = \begin{cases} 1 & , |t| < 1/2 \\ 1/2 & , |t| = 1/2 \\ 0 & , |t| > 1/2 \end{cases}$$

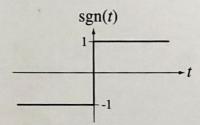
$$tri(t) = \begin{cases} 1 - |t|, & |t| < 1 \\ 0, & |t| \ge 1 \end{cases}$$

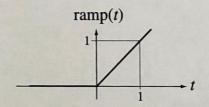
$$\operatorname{sinc}(t) = \frac{\sin(\pi t)}{\pi t}$$

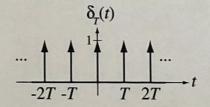
$$\operatorname{drcl}(t,N) = \frac{\sin(\pi N t)}{N \sin(\pi t)}$$

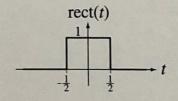


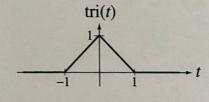


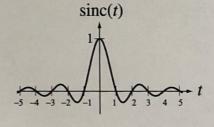


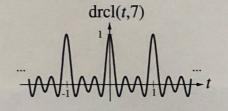






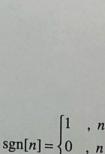






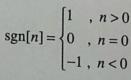


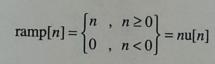


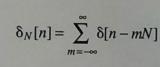


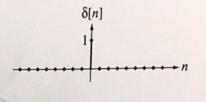
 $\delta[n] = \begin{cases} 1 & , & n=0 \\ 0 & , & n \neq 0 \end{cases}$

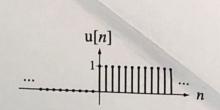
 $\mathbf{u}[n] = \begin{cases} 1 & , & n \ge 0 \\ 0 & , & n < 0 \end{cases}$

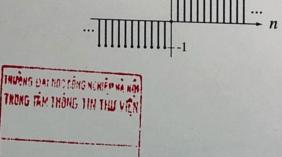




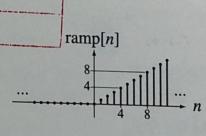


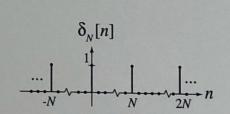






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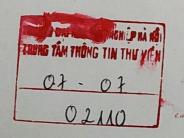


Signals and Systems

Analysis Using Transform Methods and MATLAB®
Second Edition

Michael J. Roberts

Professor, Department of Electrical and Computer Engineering University of Tennessee









SIGNALS AND SYSTEMS: ANALYSIS USING TRANSFORM METHODS AND MATLAB®. SECOND EDITION

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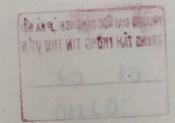
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To my wife Barbara for giving me the time and space to complete this effort and to the memory of my parents, Bertie Ellen Pinkerton and Jesse Watts Roberts, for their early emphasis on the importance of education.

Preface, xii

Chapter 1

Introduction, 1

- 1.1 Signals and Systems Defined, 1
- 1.2 Types of Signals, 3
- 1.3 Examples of Systems, 8

 A Mechanical System, 9

 A Fluid System, 9

 A Discrete-Time System, 11
 - Feedback Systems, 12
- 1.4 A Familiar Signal and System Example, 14
- 1.5 Use of MATLAB[®], 18

Chapter 2

Mathematical Description of Continuous-Time Signals, 19

- 2.1 Introduction and Goals, 19
- 2.2 Functional Notation, 20
- 2.3 Continuous-Time Signal Functions, 20

Complex Exponentials and Sinusoids, 21

Functions with Discontinuities, 23

The Signum Function, 24

The Unit-Step Function, 24

The Unit-Ramp Function, 26

The Unit Impulse, 27

The Impulse, the Unit Step and Generalized Derivatives, 29

The Equivalence Property of the Impulse, 30

The Sampling Property of the Impulse, 31

The Scaling Property of the Impulse, 31

The Unit Periodic Impulse or Impulse Train, 32

A Coordinated Notation for Singularity Functions, 33

The Unit-Rectangle Function, 33

- 2.4 Combinations of Functions, 34
- 2.5 Shifting and Scaling, 36
 Amplitude Scaling, 36
 Time Shifting, 37

Time Scaling, 39
Simultaneous Shifting and Scaling, 43

- 2.6 Differentiation and Integration, 47
- 2.7 Even and Odd Signals, 49

 Combinations of Even and Odd Signals, 51

 Derivatives and Integrals of Even and Odd Signals, 53
- 2.8 Periodic Signals, 53
- 2.9 Signal Energy and Power, 56
 Signal Energy, 56
 Signal Power, 57
- **2.10** Summary of Important Points, 60 Exercises, 60

Exercises with Answers, 60

Signal Functions, 60

Scaling and Shifting, 61

Derivatives and Integrals, 65

Even and Odd Signals, 66

Periodic Signals, 68

Signal Energy and Power, 69

Exercises without Answers, 70

Signal Functions, 70

Scaling and Shifting, 71

Generalized Derivative, 74

Derivatives and Integrals, 74

Even and Odd Signals, 75

Periodic Signals, 75

Signal Energy and Power, 76

Chapter 3

Discrete-Time Signal Description, 77

- 3.1 Introduction and Goals, 77
- 3.2 Sampling and Discrete Time, 78
- 3.3 Sinusoids and Exponentials, 80 Sinusoids, 80 Exponentials, 83
- 3.4 Singularity Functions, 84

 The Unit-Impulse Function, 84

 The Unit-Sequence Function, 85

 The Signum Function, 85

Contents

	The Unit-Ramp Function, 86		Additivity, 128
	The Unit Periodic Impulse Function or Impulse		Linearity and Superposition, 129
	Train, 86		LTI Systems, 129
3.5	Shifting and Scaling, 87		Stability, 133
	Amplitude Scaling, 87		Causality, 134
	Time Shifting, 87		Memory, 134
	Time Scaling, 87		Static Nonlinearity, 135
	Time Compression, 88		Invertibility, 137
	Time Expansion, 88		Dynamics of Second-Order Systems, 138
3.6	Differencing and Accumulation, 92		Complex Sinusoid Excitation, 140
3.7	Even and Odd Signals, 96	4.3	Discrete-Time Systems, 140
	Combinations of Even and Odd Signals, 97		System Modeling, 140
	Symmetrical Finite Summation of Even and Odd		Block Diagrams, 140
	Signals, 97		Difference Equations, 141
3.8	Periodic Signals, 98		System Properties, 147
3.9	Signal Energy and Power, 99	4.4	Summary of Important Points, 150
	Signal Energy, 99	Exe	rcises, 151
	Signal Power, 100	E	xercises with Answers, 151
3.10	Summary of Important Points, 102		System Models, 151
Exer	cises, 102		System Properties, 153
	tercises with Answers, 102	E	xercises without Answers, 155
	Signal Functions, 102		System Models, 155
	Scaling and Shifting, 104		System Properties, 157
	Differencing and Accumulation, 105		The second solven
	Even and Odd Signals, 106		
	Periodic Signals, 107	Cha	pter 5
	Signal Energy and Power, 108	Tim	e-Domain System Analysis, 159
Ex	tercises without Answers, 108	5.1	Introduction and Goals, 159
	Signal Functions, 108	5.2	Continuous Time, 159
	Shifting and Scaling, 109		Impulse Response, 159
	Differencing and Accumulation, 111		Continuous-Time Convolution, 164
	Even and Odd Signals, 111		Derivation, 164
	Periodic Signals, 112		Graphical and Analytical Examples of
	Signal Energy and Power, 112		Convolution, 168
	Description out Engineers 242 and the File		Convolution Properties, 173
Char	oter 4_		System Connections, 176
	cription of Systems, 113		Step Response and Impulse Response, 176
			Stability and Impulse Response, 176
4.1	Introduction and Goals, 113		Complex Exponential Excitation and the Transfer
4.2	Continuous-Time Systems, 114		Function, 177
	System Modeling, 114		Frequency Response, 179
	Differential Equations, 115	5.3	Discrete Time, 181
	Block Diagrams, 119		Impulse Response, 181
	System Properties, 122		Discrete-Time Convolution, 184
	Introductory Example, 122		Derivation, 184
	Homogeneity, 126		Graphical and Analytical Examples of
	Time Invariance, 127		Convolution, 187

	Convolution Properties, 191
	Numerical Convolution, 191
	Discrete-Time Numerical Convolution, 191
	Continuous-Time Numerical Convolution, 193
	Stability and Impulse Response, 195
	System Connections, 195
	Unit-Sequence Response and Impulse Response, 196
	Complex Exponential Excitation and the Transfer Function, 198
	Frequency Response, 199
5.4	Summary of Important Points, 201
Exer	rcises, 201
E	xercises with Answers, 201
	Continuous Time, 201

Impulse Response, 201

Convolution, 201

Stability, 204

Discrete Time, 205

Impulse Response, 205

Convolution, 205

Stability, 208

Exercises without Answers, 208

Continuous Time, 208

Impulse Response, 208

Convolution, 209

Stability, 210

Discrete Time, 212

Impulse Response, 212

Convolution, 212

Stability, 214

Chapter 6

6.2

Continuous-Time Fourier Methods, 215

- 6.1 Introduction and Goals, 215
- The Continuous-Time Fourier Series, 216 Conceptual Basis, 216 Orthogonality and the Harmonic Function, 220 The Compact Trigonometric Fourier Series, 223

Convergence, 225

Continuous Signals, 225

Discontinuous Signals, 226

Minimum Error of Fourier-Series Partial Sums, 228

The Fourier Series of Even and Odd Periodic Functions, 229

Fourier-Series Tables and Properties, 230

Numerical Computation of the Fourier Series, 234

6.3 The Continuous-Time Fourier Transform, 241 Extending the Fourier Series to Aperiodic Signals, 241 The Generalized Fourier Transform, 246 Fourier Transform Properties, 250 Numerical Computation of the Fourier Transform, 259

6.4 Summary of Important Points, 267

Exercises, 267

Exercises with Answers, 267

Fourier Series, 267

Orthogonality, 268

CTFS Harmonic Functions, 268

System Response to Periodic Excitation, 271

Forward and Inverse Fourier Transforms, 271

Relation of CTFS to CTFT, 280

Numerical CTFT, 281

System Response, 282

Exercises without Answers, 282

Fourier Series, 282

Orthogonality, 283

Forward and Inverse Fourier Transforms, 283

Chapter 7

Discrete-Time Fourier Methods, 290

- 7.1 Introduction and Goals, 290
- 7.2 The Discrete-Time Fourier Series and the Discrete Fourier Transform, 290 Linearity and Complex-Exponential Excitation, 290 Orthogonality and the Harmonic Function, 294 Discrete Fourier Transform Properties, 298 The Fast Fourier Transform, 302
- 7.3 The Discrete-Time Fourier Transform, 304 Extending the Discrete Fourier Transform to Aperiodic Signals, 304

Derivation and Definition, 305

The Generalized DTFT, 307

Convergence of the Discrete-Time Fourier Transform, 308

DTFT Properties, 309

Numerical Computation of the Discrete-Time Fourier Transform, 315

- 7.4 Fourier Method Comparisons, 321
- 7.5 Summary of Important Points, 323

Exercises, 323

Exercises with Answers, 323

Orthogonality, 323

Discrete Fourier Transform, 324

Contents

Discrete-Time Fourier Transform Definition, 324 Forward and Inverse Discrete-Time Fourier Transforms, 325

Exercises without Answers, 328

Discrete Fourier Transform, 328 Forward and Inverse Discrete-Time Fourier Transforms, 328

Chapter 8

The Laplace Transform, 331

- 8.1 Introduction and Goals, 331
- 8.2 Development of the Laplace Transform, 332

 Generalizing the Fourier Transform, 332

 Complex Exponential Excitation and Response, 334
- **8.3** The Transfer Function, 335
- 8.4 Cascade-Connected Systems, 335
- 8.5 Direct Form II Realization, 336
- **8.6** The Inverse Laplace Transform, 337
- 8.7 Existence of the Laplace Transform, 337

 Time-Limited Signals, 338

 Right- and Left-Sided Signals, 338
- 8.8 Laplace Transform Pairs, 339
- 8.9 Partial-Fraction Expansion, 344
- 8.10 Laplace Transform Properties, 354
- 8.11 The Unilateral Laplace Transform, 356

 Definition, 356

 Properties Unique to the Unilateral Laplace
 Transform, 358

Solution of Differential Equations with Initial Conditions, 360

- **8.12** Pole-Zero Diagrams and Frequency Response, 362
- 8.13 MATLAB System Objects, 370
- 8.14 Summary of Important Points, 372

Exercises, 372

Exercises with Answers, 372

Laplace Transform Definition, 372

Existence of the Laplace Transform, 373

Direct Form II System Realization, 373

Forward and Inverse Laplace Transforms, 373

Unilateral Laplace Transform Integral, 375

Solving Differential Equations, 376

Pole-Zero Diagrams and Frequency Response, 377

Exercises without Answers, 378

Laplace Transform Definition, 378

Existence of the Laplace Transform, 378
Direct Form II System Realization, 378
Forward and Inverse Laplace Transforms, 378
Solution of Differential Equations, 379
Pole-Zero Diagrams and Frequency Response, 380

Chapter 9

The z Transform, 382

- 9.1 Introduction and Goals, 382
- **9.2** Generalizing the Discrete-Time Fourier Transform, 383
- **9.3** Complex Exponential Excitation and Response, 384
- **9.4** The Transfer Function, 384
- 9.5 Cascade-Connected Systems, 384
- 9.6 Direct Form II System Realization, 385
- 9.7 The Inverse z Transform, 386
- 9.8 Existence of the z Transform, 386

 Time-Limited Signals, 386

 Right- and Left-Sided Signals, 387
- 9.9 z-Transform Pairs, 389
- 9.10 z-Transform Properties, 392
- 9.11 Inverse z-Transform Methods, 393
 Synthetic Division, 393
 Partial-Fraction Expansion, 394
 Examples of Forward and Inverse z Transforms, 394
- 9.12 The Unilateral z Transform, 399

 Properties Unique to the Unilateral z Transform, 399

 Solution of Difference Equations, 400
- **9.13** Pole-Zero Diagrams and Frequency Response, 401
- 9.14 MATLAB System Objects, 404
- 9.15 Transform Method Comparisons, 406
- **9.16** Summary of Important Points, 410 Exercises, 411

Exercises with Answers, 411

Direct Form II System Realization, 411

Existence of the z Transform, 411

Forward and Inverse z Transforms, 411

Unilateral z-Transform Properties, 413 Solution of Difference Equations, 414

Pole-Zero Diagrams and Frequency Response, 415

Exercises without Answers, 416

Direct Form II System Realization, 416 Existence of the z Transform, 416 Forward and Inverse z Transforms, 416 Pole-Zero Diagrams and Frequency Response, 417

Chapter 10

Sampling and Signal Processing, 420

10.1 Introduction and Goals, 420

10.2 Continuous-Time Sampling, 421

Sampling Methods, 421

The Sampling Theorem, 423

Qualitative Concepts, 423

Sampling Theorem Derivation, 425

Aliasing, 428

Time-Limited and Bandlimited Signals, 431

Interpolation, 432

Ideal Interpolation, 432

Practical Interpolation, 433

Zero-Order Hold, 434

First-Order Hold, 434

Sampling Bandpass Signals, 435

Sampling a Sinusoid, 438

Band-Limited Periodic Signals, 441

Signal Processing Using the DFT, 444

CTFT-DFT Relationship, 444

CTFT-DTFT Relationship, 445

Sampling and Periodic-Repetition

Relationship, 448

Computing the CTFS Harmonic Function

with the DFT, 452

Approximating the CTFT with the DFT, 452

Forward CTFT, 452

Inverse CTFT, 453

Approximating the DTFT with the DFT, 453

Approximating Continuous-Time Convolution

with the DFT, 453

Aperiodic Convolution, 453

Periodic Convolution, 453

Discrete-Time Convolution with the DFT. 453

Aperiodic Convolution, 453

Periodic Convolution, 453

Summary of Signal Processing Using the DFT, 454

10.3 Discrete-Time Sampling, 455

Periodic-Impulse Sampling, 455

Interpolation, 457

10.4 Summary of Important Points, 460

Exercises, 461

Exercises with Answers, 461

Pulse Amplitude Modulation, 461

Sampling, 461

Impulse Sampling, 462

Nyquist Rates, 465

Time-Limited and Bandlimited Signals, 465

Interpolation, 466

Aliasing, 467

Bandlimited Periodic Signals, 468

CTFT-CTFS-DFT Relationships, 468

Windows, 470

DFT, 471

Exercises without Answers, 475

Sampling, 475

Impulse Sampling, 476

Nyquist Rates, 477

Aliasing, 477

Practical Sampling, 477

Bandlimited Periodic Signals, 478

DFT, 478

Chapter 11

Frequency Response Analysis, 481

- 11.1 Introduction and Goals, 481
- 11.2 Frequency Response, 481
- 11.3 Continuous-Time Filters, 482

Examples of Filters, 482

Ideal Filters, 487

Distortion, 487

Filter Classifications, 488

Ideal Filter Frequency Responses, 488

Impulse Responses and Causality, 489

The Power Spectrum, 492

Noise Removal, 492

Bode Diagrams, 493

The Decibel, 493

The One-Real-Pole System, 497

The One-Real-Zero System, 498

Integrators and Differentiators, 499

Frequency-Independent Gain, 499

Complex Pole and Zero Pairs, 502

Practical Filters, 504

Passive Filters, 504

The Lowpass Filter, 504

The Bandpass Filter, 507

Contents

Operational Amplifiers, 509 The Integrator, 510 The Lowpass Filter, 510 11.4 Discrete-Time Filters, 518 Notation, 518 Ideal Filters, 519 Distortion, 519 Filter Classifications, 520 Frequency Responses, 520 Impulse Responses and Causality, 520 Filtering Images, 521 Practical Filters, 526 Comparison with Continuous-Time Filters, 526 Highpass, Bandpass and Bandstop Filters, 528 The Moving Average Filter, 532 The Almost Ideal Lowpass Filter, 536 Advantages Compared to Continuous-Time Filters, 538 11.5 Summary of Important Points, 538 Exercises, 539 Exercises with Answers, 539 Continuous-Time Frequency Response, 539 Continuous-Time Ideal Filters, 539 Continuous-Time Causality, 540 Logarithmic Graphs and Bode Diagrams, 540 Continuous-Time Practical Passive Filters, 541 Continuous-Time Practical Active Filters, 544 Discrete-Time Frequency Response, 545 Discrete-Time Ideal Filters, 546 Discrete-Time Causality, 546 Discrete-Time Practical Filters, 546 Exercises without Answers, 547 Continuous-Time Frequency Response, 547 Continuous-Time Ideal Filters, 547 Continuous-Time Causality, 548 Bode Diagrams, 548 Continuous-Time Practical Passive Filters, 549 Continuous-Time Filters, 551 Continuous-Time Practical Active Filters, 551 Discrete-Time Causality, 554 Discrete-Time Filters, 554 Image Filtering, 557

Active Filters, 508

Chapter 12

Communication System Analysis, 558

- 12.1 Introduction and Goals, 558
- 12.2 Continuous Time Communication Systems, 558

Need for Communication Systems, 558

Frequency Multiplexing, 560

Analog Modulation and Demodulation, 561

Amplitude Modulation, 561

Double-Sideband Suppressed-Carrier

Modulation, 561

Double-Sideband Transmitted-Carrier

Modulation, 564

Single-Sideband Suppressed-Carrier

Modulation, 566

Angle Modulation, 567

- **12.3** Discrete-Time Sinusoidal-Carrier Amplitude Modulation, 576
- **12.4** Summary of Important Points, 578

Exercises, 578

Exercises with Answers, 578

Amplitude Modulation, 578

Angle Modulation, 580

Exercises without Answers, 582

Amplitude Modulation, 582

Angle Modulation, 583

Envelope Detector, 583

Chopper-Stabilized Amplifier, 584

Multipath, 585

Chapter 13

Laplace System Analysis, 586

- 13.1 Introduction and Goals, 586
- 13.2 System Representations, 586
- 13.3 System Stability, 590
- 13.4 System Connections, 593

Cascade and Parallel Connections, 593

The Feedback Connection, 593

Terminology and Basic Relationships, 593

Feedback Effects on Stability, 594

Beneficial Effects of Feedback, 595

Instability Caused by Feedback, 598

Stable Oscillation Using Feedback, 602

The Root-Locus Method, 606

Tracking Errors in Unity-Gain Feedback Systems, 612

14.7 Standard Realizations of Systems, 661

Cascade Realization, 661
Parallel Realization, 661

13.5 System Analysis Using MATLAB, 615	14.8 Summary of Important Points, 662	
13.6 System Responses to Standard Signals, 617	Exercises, 663	
Unit-Step Response, 618	Exercises with Answers, 663	
Sinusoid Response, 621	Stability, 663	
13.7 Standard Realizations of Systems, 624	Parallel, Cascade and Feedback Connections, 663	
Cascade Realization, 624	Response to Standard Signals, 663	
Parallel Realization, 626	Root Locus, 664	
13.8 Summary of Important Points, 626	Laplace-Transform-z-Transform Relationship, 665	
Exercises, 627	Sampled-Data Systems, 665	
Exercises with Answers, 627	System Realization, 665	
Transfer Functions, 627	Exercises without Answers, 666	
Stability, 628	Stability, 666	
Parallel, Cascade and Feedback Connections, 629	Parallel, Cascade and Feedback Connections, 666	
Root Locus, 631	Response to Standard Signals, 667	
Tracking Errors in Unity-Gain Feedback Systems, 632	Laplace-Transform-z-Transform Relationship, 668	
Response to Standard Signals, 632	Sampled-Data Systems, 668	
System Realization, 633	System Realization, 668	
Exercises without Answers, 634	General, 669	
Transfer Functions, 634		
Stability, 634	And the second s	
Parallel, Cascade and Feedback Connections, 634	Chapter 15 Filter Analysis and Design, 670	
Root Locus, 638		
Tracking Errors in Unity-Gain Feedback Systems, 639	15.1 Introduction and Goals, 670	
Responses to Standard Signals, 639	15.2 Analog Filters, 670	
System Realization, 640	Butterworth Filters, 671	
	Normalized Butterworth Filters, 671	
Chapter 14	Filter Transformations, 672	
z-Transform System Analysis, 641	MATLAB Design Tools, 674	
2-11 ansiot in System Analysis, 041	Chebyshev, Elliptic and Bessel Filters, 676	
14.1 Introduction and Goals, 641	15.3 Digital Filters, 679	
14.2 System Models, 641	Simulation of Analog Filters, 679	
Difference Equations, 641	Filter Design Techniques, 679	
Block Diagrams, 642	IIR Filter Design, 679	
14.3 System Stability, 642	Time-Domain Methods, 679	
14.4 System Connections, 643	Impulse-Invariant Design, 679	
14.5 System Responses to Standard Signals, 645	Step-Invariant Design, 686	
Unit-Sequence Response, 645	Finite-Difference Design, 688	
Response to a Causal Sinusoid, 648	Frequency-Domain Methods, 694	
14.6 Simulating Continuous-Time Systems with	Direct Substitution and the Matched	
Discrete-Time Systems, 651	z-Transform, 694	
z-Transform-Laplace-Transform Relationships, 651	The Bilinear Method, 696	
Impulse Invariance, 653	FIR Filter Design, 703	
Sampled-Data Systems, 655	Truncated Ideal Impulse Response 703	

Optimal FIR Filter Design, 713

MATLAB Design Tools, 715

15.4 Summary of Important Points, 717

Exercises, 717

Exercises with Answers, 717

Continuous-Time Butterworth Filters, 717

Impulse-Invariant and Step-Invariant Filter Design, 719

Finite-Difference Filter Design, 720

Matched z-Transform and Direct Substitution

Filter Design, 720

Bilinear z-Transform Filter Design, 721

FIR Filter Design, 721

Exercises without Answers, 723

Analog Filter Design, 723

Impulse-Invariant and Step-Invariant Filter Design, 724

Finite-Difference Filter Design, 724

Matched z-Transform and Direct Substitution Filter

Design, 724

Bilinear z-Transform Filter Design, 725

FIR Filter Design, 725

Chapter 16

State-Space Analysis, 726

16.1 Introduction and Goals, 726

16.2 Continuous-Time Systems, 726

System and Output Equations, 727

Transfer Functions, 738

Alternate State-Variable Choices, 740

Transformations of State Variables, 741

Diagonalization, 742

MATLAB Tools for State-Space Analysis, 745

16.3 Discrete-Time Systems, 746

System and Output Equations, 746

Transfer Functions and Transformations of State

Variables, 750

MATLAB Tools for State-Space Analysis, 753

16.4 Summary of Important Points, 753

Exercises, 754

Exercises with Answers, 754

Continuous-Time State Equations, 754

Continuous-Time System Response, 756

Diagonalization, 756

Differential-Equation Description, 757

Discrete-Time State Equations, 757

Difference-Equation Description, 758

Discrete-Time System Response, 758

Exercises without Answers, 759

Continuous-Time State Equations, 759

Continuous-Time System Response, 759

Discrete-Time State Equations, 759

Discrete-Time System Response, 760

Diagonalization, 760

Appendix A Usef

Useful Mathematical

Relations, 761

B Continuous-Time Fourier Series

Pairs, 764

C Discrete Fourier Transform

Pairs, 767

D Continuous-Time Fourier Transform

Pairs, 770

E Discrete-Time Fourier Transform

Pairs, 777

F Tables of Laplace Transform

Pairs, 782

G z Transform Pairs, 784

Bibliography, 786

Index, 788